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## Fifth Semester B.E. Degree Examination, December 2010 Digital Signal Processing

Time: 3 hrs.

Max. Marks:100

**Note: Answer any FIVE full questions.**

- 1 a. State and prove the following properties of DFT:
  - i) Frequency shift      ii) Convolution in time domain      iii) Linearity. (12 Marks)
- b. Evaluate the circular convolution of the two sequences
 
$$x_1(n) = \{ 1, 2, 3, 1 \}$$

$$x_2(n) = \{ 4, 3, 2, 2 \}$$
(08 Marks)
  
- 2 a. Compute 6-point DFT of  $x(n) = \cos \frac{2\pi}{6} \cdot n$  (10 Marks)
- b. Let  $x(n)$  be N-point real sequence with N-point DFT,  $X(k)$  (N even). In addition,  $x(n)$  satisfies the following symmetry property:
 
$$x\left(n + \frac{N}{2}\right) = -x(n), \quad n = 0, 1, 2, \dots, \frac{N}{2} - 1$$

Show that  $X(k) = 0$  for k even. (10 Marks)
  
- 3 a. Compute 8-point DFT using DIT-FFT algorithm
 
$$x(n) = \cos \frac{\pi}{2} \cdot n$$
- b. Draw the computational flow diagram and indicate all intermediate values. (12 Marks)
- c. Explain the DSP processor TMS320 architecture. (08 Marks)
  
- 4 a. Consider 8-point DIT-FFT flow diagram (graph):
  - i) What is the gain of the signal path that goes from  $x(7)$  to  $X(2)$ .
  - ii) Write an expression for  $X(3)$  using the operation indicated by signal flow graph. (10 Marks)
- b. Explain the decimation-in-frequency algorithm for 8-point FFT computation. (10 Marks)
  
- 5 a. Transform the single pole lowpass Butterworth filter with system function  $H(s) = \frac{\Omega_p}{s + \Omega_p}$  into a highpass filter of cutoff frequency  $\Omega_c$  and a bandpass filter with band edge frequencies  $\Omega_{c1}$  and  $\Omega_{c2}$ . (08 Marks)
- b. Derive an expression for frequency response (magnitude and phase response) of symmetric FIR filter for odd and even length. (12 Marks)
  
- 6 a. Design a digital symmetric lowpass linear phase FIR filter having desired frequency response
 
$$H_d(w) = \begin{cases} e^{-j2w} & 0 \leq |w| \leq \pi/2 \\ 0 & \text{Otherwise} \end{cases}$$
- b. Employ hamming window of length 5. (14 Marks)  
Compare FIR and IIR filters. (06 Marks)

2. Any revealing of identification, appeal to evaluator and/or equations written eg. 42, 48 - 50, will be treated as malpractice.

7 Design a digital lowpass filter to meet the following specifications:

- Passband ripple :  $\leq 1$  dB  
 Passband edge : 4 kHz  
 Stopband attenuation:  $\geq 20$  dB  
 Stopband edge : 6 kHz  
 Sampling rate : 24 kHz

The filter is to be designed using bilinear transformation on analog Butterworth system functions. (20 Marks)

8 a. Obtain Direct-form-I, Direct-form-II, cascade and parallel structures for the system function (15 Marks)

$$H(z) = \frac{2(1-z^{-1})(1+\sqrt{2}z^{-1}+z^{-2})}{(1+0.5z^{-1})(1-0.9z^{-1}+0.81z^{-2})}$$

b. Realize the system function  $H(z) = 1 + \frac{3}{2}z^{-1} + \frac{4}{5}z^{-2} + \frac{5}{9}z^{-3} + \frac{1}{9}z^{-4}$  using direct form II. (05 Marks)

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